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# Testing for Bubbles in Stock Markets With Irregular Dividend Distribution<sup>1</sup>

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### Testing for Bubbles in Stock Markets With Irregular Dividend Distribution

#### **Itamar Caspi and Meital Graham**

#### **Abstract**

Recursive right-tailed unit root tests have recently become a popular tool to test the existence of stock price bubbles. These tests require continuous data on dividend distribution that is not always available, in particular when it comes to sectoral indexes or individual stocks. In this paper we show that it is possible to circumvent this problem by applying the test to an equity bubble using the book-to-market ratio. We illustrate our framework by testing for a bubble in the Israeli stock market, where data on continuous dividend distribution are uncommon.

Keywords: Bubbles, stock markets, book-to-market, explosive root, GSADF test, Israel JEL Classification: C12, C15, G12, G15

מבחן לבועה במחירי המניות כאשר חלוקת הדיווידנד אינה רציפה: יישום על שוק המניות הישראלי

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#### תקציר

מחקר זה נועד לבחון אם אפשר לזהות – בהווה ובעבר – בועה במחירי המניות בשוק ההון הישראלי. לשם כך אנו משתמשים במבחנים אקונומטריים לזיהוי בועות במחירי נכסים ולמעקב אחריהן. יישום המבחנים על נתוני שוק ההון הישראלי כרוך באתגר, מאחר ששוק זה אינו מתאפיין בחלוקת דיווידנדים רציפה. במחקר אנו מראים כי אפשר ליישמם תוך שימוש בנתונים על מכפילי ההון. תקופת המדגם שלנו משתרעת מיולי 1996 עד נובמבר 2014, ובתקופה זו תוצאות המבחנים אינן מעלות עדות חד-משמעית לבועה בענף או במדד כלשהו של שוק המניות הישראלי.

### 1. Introduction

Asset price bubbles, and stock price bubbles in particular, have gained a tremendous amount of attention both in public discussion and in academia. Recent empirical work suggests that such bubbles might have devastating consequences for the economy, especially when coupled with a credit boom (Jordà et al., 2015, 2016). The most recent example of such a phenomenon is the "Dot-com" bubble of the 1990s during which advanced economies' stock prices, mostly related to the rapidly growing Internet sector, surged, only to witness a sharp reversal during the late 1990s—early 2000s. As its name suggests, this boom and bust period in Internet stock prices is perceived as a bubble, suggesting that the surge in prices was mostly speculative in nature and unrelated to fundamentals. Nonetheless, at least in academia, the mere existence of bubbles, let alone the ability to detect them in real time, remains in debate.

In recent years, new econometric methods that aim at testing the existence and prevalence of bubble periods, attracted a great deal of attention in the literature. One prominent strand of this literature, initiated by Phillips et al. (2011) and Phillips et al. (2015), applies time series methods in order to detect and date-stamp bubbles. The key innovation is the use of recursive right-tailed unit root tests. These exhibit good power properties against the alternative of a bubble, are often used as a real time monitoring device for bubbles (e.g., Homm and Breitung, 2012), and have many applications in various markets – from stocks through commodities to housing markets.

in order to test for a bubble in stock prices, the literature initiated by Phillips et al. (2011) usually uses data on prices and dividends and tests whether the former is explosive while the latter is not or whether the ratio between them is explosive. Examples include Phillips et al. (2011) who investigate the Nasdaq composite price index and the Nasdaq composite dividend; Phillips et al. (2015) who analyze the S&P 500 price-to-dividend ratio; Homm and Breitung (2012) who test the Nikkei 225, FTSE 100, Hang Seng, and Shanghai indexes<sup>1</sup>; Christensen and Andersen (2015) who test price-to-dividend ratios from a panel of 23 countries; and Chang et al. (2016) who test the Brazil, Russia, India, China and South Africa (BRICS) stock price-dividend ratios. The above examples highlight the fact that testing for the existence of bubbles is deeply dependent on the availability of a continuous dividend series. Hence, using these tests to determine the existence of a bubble in

 $<sup>^1</sup>Homm$  and Breitung (2012) note that dividend series were only available for the S&P 500 and the Hang Seng.

individual stocks or markets where the distribution of dividends is not continuous are bubbly is challenging.

The purpose of this paper is to provide a framework that allows the implementation of the Phillips et al. (2011) and Phillips et al. (2015) tests for bubbles in cases where data on dividends are discontinuous or even missing. In particular, instead of testing for explosiveness in prices and dividends (or in the price-to-dividend ratio), we apply the standard test to the more readily available book-to-market ratio data, and provide a theoretical justification, based on the dynamic book-to-market model (Vuolteenaho, 1999, 2002). Accordingly, explosive behavior in the book-to-market ratio may serve as evidence for an asset price bubble.

We illustrate the use of our proposed method by applying the tests for bubbles to data from the Israeli stock market (July 1996 to November 2014). The Israeli stock market is chosen due to the usual tendency of this market not to distribute dividends continuously. We find no evidence of bubble periods in any of the sectors we examine. Our empirical application in this study is related to a series of recent studies that ask whether leading equity indices around the world exhibit bubble behavior.

The article is structured as follows. Section 2 describes the dynamic book-to-market model and provides the theoretical justification for using it to tests for bubbles. Section 3 briefly describes the bubble detection methodology. Section 4 illustrates our proposed framework by an empirical application to Israeli book-to-market data, and Section 5 concludes.

## 2. Bubbles and the Book-to-Market ratio

According to the standard present-value model, the general solution to the price of an asset is given by

$$P_t = \mathbb{E}_t \sum_{j=1}^{\infty} (1+R)^{-1} D_{t+j+1} + B_t, \tag{1}$$

where  $P_t$  denotes the price of an asset at time t,  $D_t$  the dividend, R a constant discount rate,  $\mathbb{E}_t$  the mathematical expectation conditioned on information at time t, and  $B_t$  the rational bubble component that satisfies

$$\mathbb{E}_t[B_{t+1}] = (1+R)B_t. \tag{2}$$

The first component on the right-hand side of Equation 1 is the "fundamental value." When no bubble exists, i.e., when  $B_t = 0$ , the price reflects the fundamental value. Conversely,  $B_t \neq 0$  describes a situation where investors are willing to pay a premium over the fundamental value. According to condition (2), paying such a premium is justified since it is expected to increase at a rate of 1 + R over the next period.

Since the discount rate is strictly positive, Equation (2) implies that the  $B_t$  follows an *explosive* path. Moreover, if an explosive bubble is present it will eventually dominate the stochastic behavior of  $P_t$ , which will be explosive as well. In effect, the explosiveness feature of the bubble component provides an identifying restriction that can be used to empirically test for the presence of a bubble. In particular, finding that  $P_t$  is explosive while  $D_t$  is not may serve as evidence for the presence of a bubble.

Testing for a bubble in equities for which dividends data are discontinuous is technically impossible To tackle this problem, we suggest using the book-to-market model of Vuolteenaho (1999, 2002), that starts off with the identity

$$V_t - V_{t-1} = X_t - D_t, (3)$$

where  $V_t$  denotes the book value at time t,  $X_t$  the earnings, and  $D_t$  the dividends. According to this identity the change in book value from time t-1 to t equals earnings less dividends.

Vuolteenaho continues with the definition of the log book-to-market ratio

$$vm_t = \log(V_t/M_t) = v_t - m_t, \tag{4}$$

where  $M_t$  denotes the market equity value at time t, and derives an expression for the log book-to-market ratio that is analogous to the dynamic Gordon growth model (Campbell and Shiller, 1988):

$$vm_{t} = k_{t} + \mathbb{E}_{t} \sum_{j=1}^{\infty} \rho^{j} r_{t+j+1} - \mathbb{E}_{t} \sum_{j=1}^{\infty} \rho^{j} (r_{t+j+1}^{e} - r_{t+j+1}^{f}) + b_{t},$$
 (5)

where  $r_t$  denotes the log gross extra return over market valuation at time t,  $r_t^e$  the log gross return on equity (ROE),  $r_t^f$  the log gross risk-free return,  $k_t$  a function of the constants around which the log-linear approximation is made, and  $b_t$  the

bubble component.<sup>2</sup>

Analogously to Equation (1), the first component on the right-hand side of Equation (5) is the "fundamental (log) book-to-market ratio" since it is a function of the fundamentals that determine the fundamental value of an equity, namely, ROE, risk-free return, and expected risk premiums. In turn, the second term on the right-hand side of Equation (5) represents the rational bubble component. Accordingly, the existence of a bubble is consistent with a situation where the log of the market value of a firm departs explosively from its log book value.

## 3. Econometric framework

Phillips et al. (2015, hereinafter, PSY) develop a bubble detection and date-stamping strategy that is based on tests for an explosive root. The authors set the data-generating process for the null hypothesis as a random walk with a marginally negligible drift:

$$H_0: y_t = d_T + y_{t+1} + \varepsilon_t,$$
 (6)

where  $d_T = dT^{-\eta}$  with  $\eta > 0.5$ . The alternative hypothesis is expressed as process with a mildly explosive root in the sense of Phillips and Magdalinos (2007):

$$H_1: y_t = \delta_T y_{t-1} + \varepsilon_t, \tag{7}$$

where  $\delta_T = 1 + cT^{-\theta}$  with c > 0 and  $0 < \lambda < 1$ .

The PSY methodology involves a recursive estimation of the regression model

$$\Delta y_t = \alpha_{\lambda_1, \lambda_2} + \rho_{\lambda_1, \lambda_2} y_{t-1} + \sum_{j=1}^{p-1} \gamma_{\lambda_1, \lambda_2}^i \Delta y_{t-i} + \varepsilon_t$$
 (8)

and calculation of the t-statistic

$$ADF_{\lambda_1,\lambda_2} = \frac{\hat{\rho}_{\lambda_1,\lambda_2}}{S.E.(\hat{\rho}_{\lambda_1,\lambda_2})},\tag{9}$$

where the sub- and superscripts  $\lambda_1$  and  $\lambda_2$  attached to each coefficient denote the fraction of the sample these parameters are estimated with, such that  $0 \le \lambda_1 < \lambda_2 \le 1$ . For example,  $\alpha_{\lambda_1,\lambda_2}$  is the constant term for the regression that is estimated

<sup>&</sup>lt;sup>2</sup>Here, we depart from Vuolteenaho (1999, 2002), who explicitly excludes the existence of a bubble by imposing the "value relevance" assumption that  $v_t$  and  $m_t$  are cointegrated with a cointegrating vector (1-1).

between  $\lfloor T\lambda_1 \rfloor$  and  $\lfloor T\lambda_2 \rfloor$ , where  $\lfloor \cdot \rfloor$  is the floor function.

According to PSY, the test statistic used to test the null hypothesis of "no bubble" is the Generalized Sup ADF (GSADF) test statistic, which is the supremum value of the sequence of  $ADF_{\lambda_1,\lambda_2}$  test statistics:

$$GSADF(\lambda_0) = \sup_{\substack{\lambda_2 \in [\lambda_0, 1] \\ \lambda_1 \in [0, \lambda_2 - \lambda_0]}} \{ADF_{\lambda_1, \lambda_2}\}.$$
(10)

The null is rejected when the value of the GSADF statistic exceeds the relevant critical value.

Conditioned on the null hypothesis being rejected, the estimates of the bubble period are given by

$$\hat{\lambda}_e = \inf_{\lambda_2 \in [\lambda_0, 1]} \left\{ \lambda_2 : BSADF_{\lambda_2}(\lambda_0) > cv_{r_2}^{\beta_{T\lambda_2}} \right\}$$
 (11)

$$\hat{\lambda}_f = \inf_{\lambda_2 \in [\hat{\lambda}_e, 1]} \left\{ \lambda_2 : BSADF_{\lambda_2}(\lambda_0) < cv_{\lambda_2}^{\beta_{T\lambda_2}} \right\}$$
 (12)

where BSADF( $r_0$ ) for  $r_2 \in [r_0, 1]$  is the backward sup ADF statistic defined as

$$GSADF(\lambda_0) = \sup_{\lambda_2 \in [\lambda_0, 1]} \{BSADF_{\lambda_2}(\lambda_0)\}$$
(13)

and  $cv_{\lambda_2}^{\beta_T}$  is the 100(1 –  $\beta_T$ )% critical value of the sup ADF statistic based on  $[T\lambda_2]$  observations.

# 4. Empirical application

In this section we illustrate the use of our proposed method with an empirical application to the Israeli stock market, where discontinuous dividend distribution is common and where data on book-to-market ratios is readily available. To be able to fit the dynamic book-to-market model we define the book-to-market ratio as the ratio of a company's market valuation to its equity, where equity is defined as the surplus shareholders are entitled to if the firm realizes all its assets and pays off all its liabilities.

### 4.1. Data and specifications

In our implementation we use monthly data on seven sectoral book-to-market ratios, as well as the aggregate book-to-market ratio for the period July 1996 to November 2014.<sup>3</sup> The sample in our possession is composed of 583 companies (average during the sample period) that belong to seven sectors: Insurance, Banking, Investment and Holdings, Oil and Gas Exploration, Commerce and Services, Real Estate and Construction, and Manufacturing.

Table 1 provides the sample mean for market value, book value and book-to-market ratio (along with its standard deviation) for each sector and the aggregate during the sample period.<sup>4</sup> Sizable differences are found between the sectors in both the average size and the standard deviation of the ratio, as can be seen in Figure 1, which plots the time path of the sectoral book-to-market ratios. The Oil and Gas Exploration sector had both the highest average ratio and the largest S.D. (avg. 2.67, maximum 8.14).

**Table 1** *Summary statistics by sectors* 

Sector	Market value (NIS billion)	Book value (NIS billion)	Book-to-market ratio	(std. err.)
	(1)	(2)	(3)	(4)
Insurance	14.9	10.9	1.4	(0.4)
Banking	50.4	62.6	0.8	(0.2)
Investment and holdings	48.4	60.8	0.7	(0.2)
Oil and gas exploration	12.8	3.1	2.6	(1.9)
Commerce and services	56.6	32.3	1.7	(0.5)
Real estate and construction	35.4	53.5	0.7	(0.2)
Manufacturing	197.0	86.0	2.3	(0.6)
Aggregate	419.8	311.6	1.3	(0.3)

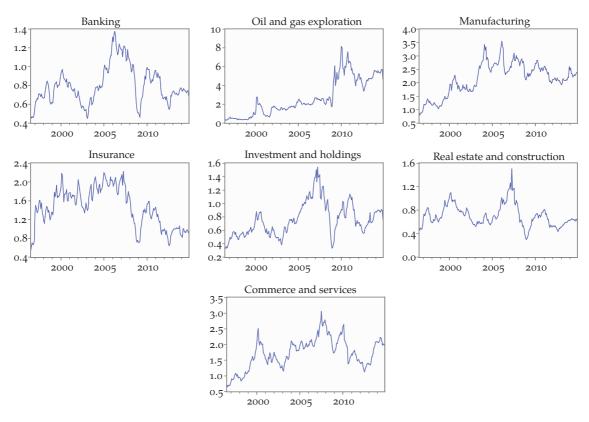
*Notes*: Multi-annual average, July 1996–November 2014. Standard errors (column 4) are for the book-to-market ratios.

All regression models used to derive the GSADF statistic include a constant. The number of lags in each equation is individually set for each sector on the basis of the BIC. The minimal window size is set according to the rule  $\lambda_0 = 0.01 + 1.8/\sqrt{T}$  (see, Phillips et al., 2015). p-values for the test are calculated via Monte Carlo simulations and using the wild bootstrap method that is suggested in Harvey et al.

<sup>&</sup>lt;sup>3</sup>The sample period covered is chosen due to data limitations.

<sup>&</sup>lt;sup>4</sup>Since the Israeli Stock Exchange canceled several sectors and established new ones over the years, many firms switched sectors during the review period. To keep this from affecting changes in the sectoral data, we made several adjustments.

Figure 1
Sectoral book-to-market ratios



Notes: July 1996-November 2014.

(2015), which is found to be robust in the presence of potential non-stationary volatility. All simulations are conducted using the Rtadf EViews add-in (Caspi, 2015), and are based on 1,999 replications.

# 4.2. Results

Table 2 shows the results of the PSY procedure for each sectoral book-to-market ratio and at the aggregate, along with Monte Carlo (third column) and wild bootstrap (fourth column) p-values. The null hypothesis (nonexistence of a bubble) is not rejected in any of the seven sectors, nor at the aggregate at a significance level of at least 10 percent, with the exception of the insurance sector, whose p-value is 9.1 percent under the Monte Carlo simulations.

Being unable to reject the null hypothesis of no bubble precludes the need to proceed to the date-stamping procedure. Nonetheless, we feel that a visual inspection of the date-stamping procedure, shown in Figure 2, is illuminating. As we can see, the BSADF sequence does cross the threshold of rejection (dashed,

 Table 2

 Results of the GSADF test for sector- level log book-to-market ratios

Sector	GSADF statistic	<i>p</i> -value	
		Monte Carlo <sup>a</sup> (1)	wild bootstrap <sup>b</sup> (2)
Banking	1.804	0.111	0.246
Oil and gas exploration	1.703	0.145	0.490
Manufacturing	1.626	0.172	0.261
Insurance	1.887	0.091	0.196
Investment and holdings	1.667	0.155	0.370
Real estate and construction	1.232	0.371	0.454
Commerce and services	1.856	0.102	0.176
Aggregate	1.073	0.487	0.523

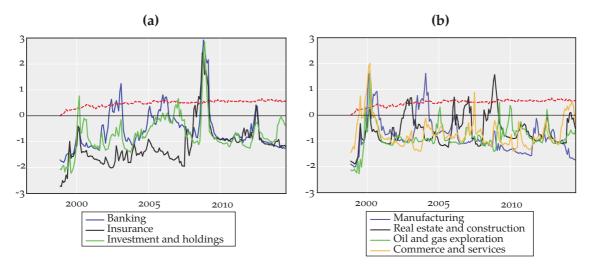
*Notes*: The GSADF statistic for the log book-to-market ratios for each sector and the aggregate, estimated over July 1996 to November 2014.

red) for some of the sectors. For example, the BSADF sequence for all three financial sectors (banking, insurance, and investment and holdings) crosses the threshold and stays above it for a few months at in and around 2008 (see panel (a) of the figure). This is of course indicative of the crash that followed the global financial crisis of 2008. This demonstrates the fact that the test we use is agnostic about the *direction* of explosiveness: positive (bubble) as well as negative (crash) explosiveness may cause rejection. Thus, it is up to the researcher to use some discretion before calling a period a bubble. Moreover, the run-up phase of a bubble is likely to be long and gradual. Thus, "blips," i.e., short episodes where the BSADF sequence stays above the threshold, should be ruled out a priori as indicative of a bubble.

<sup>&</sup>lt;sup>a</sup> The DGP for the null hypothesis is Equation (6), where  $d = \eta = 1$  and  $\varepsilon_t \sim \text{i.i.d. } N(0, 1)$ .

<sup>&</sup>lt;sup>b</sup> Based on the wild bootstrap (Harvey et al., 2015).

**Figure 2** *Results of the date-stamping procedure* 



# 5. Conclusions

In this paper we show how to apply the SADF and GSADF tests for bubbles (Phillips and Yu, 2011; Phillips et al., 2015) in cases where dividend data are absent. Our method is based on the dynamic book-to-market ratio model of Vuolteenaho (1999, 2002), which predicts that in the presence of a bubble, the log book-to-market ratio exhibits explosive behavior; i.e., it follows a stochastic process with a root that is greater than unity. We illustrate our framework with an empirical application to the Israeli stock market, where dividends are distributed irregularly. Using data on Israeli book-to-market ratios from July 1996 to August 2014, we find no evidence of the existence of a bubble. Our results are shown to be robust to the potential presence of non-stationary volatility.

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